DONNAN DIALYSIS ASSISTED BY INTERPENETRATING POLYMER NETWORKS FOR CHROMIUM ION TRANSPORT IN AQUEOUS MEDIA

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ABSTRACT

Macroporous polypropylene (MPP) membranes incorporating poly[sodium (styrene sulphonate)], P(SSNa), and poly[ar-vinylbenzyl] trimethylammonium chloride], P(ClVBTA) were modified via “in situ” radical polymerization. Modified and unmodified MPP were characterized using SEM and charge density properties. Donnan dialysis was used to transport chromium ions. The results show that the degree of modification varied between 2.5% and 4.0%, and the water uptake percentage varied between 15% and 20%. Experimental data for chromium ion transport (Cr(III) and Cr(VI)) were fitted to a mathematical model, and a correlation coefficient very close to 1 was obtained. The main parameters of this mathematical fit are k and a. These parameters represent the concentration of chromium ions that converge in the Donnan equilibrium (k) and the response rate of the modified membrane (a).

Keywords: Chromium, Donnan dialysis, interpenetrating polymer network, mathematical model, polypropylene.

INTRODUCTION

Many serious environmental problems are caused by water sources that are polluted by metal and metalloid ions. Chromium, mercury, copper, nickel, cadmium, and arsenic are among these contaminating species. Different oxidation states are presented by chromium ions in water, such as trivalent chromium Cr(III) and hexavalent chromium Cr(VI). Cr(VI) is one of the most toxic ion species because it can cause cancer and other serious health problems. These problems depend on the concentration and exposure period.1

Cr(VI) ions accumulate in biological systems and are water soluble at all pHs. Recommendations are given by the World Health Organization, where a limit of 0.05 mg L⁻¹ for Cr(VI) or Cr(III) is accepted as the maximum permissible concentration.2

Concentration and pH are important factors for the speciation of Cr(VI) that exists as oxanions. At the pH range between 0.75 until 6.45, the main chromium dominant ions are: chromic acid (H₂CrO₄), it is the strong acid (H, Cr₂O₇⁻→HCrO₄⁻, K=10⁻¹²), acid chromate (HCrO₄⁻), it is deprotonated forms in solutions where has been low concentration of Cr(VI) less than 0.01 g L⁻¹ (HCrO₄⁻→H⁺+HCrO₄⁻, K=10⁻¹⁰⁻⁴), dichromate (Cr₂O₇²⁻), it is the polymerized form of the (HCrO₄⁻) when the Cr(VI) concentration is on the 10⁻⁴ mol L⁻¹ (2HCrO₄⁻→Cr₂O₇²⁻+H₂O,K=10⁻⁰⁵) and dichromate acid (H₂CrO₄⁻), but only if the solution is strongly acidic and the concentration of Cr(VI) ion is high.3

Above pH 6.45, is found a high quantity of chromate (CrO₄²⁻) ions throughout the concentration range.4

Cr(III) is an essential element for life, although at certain concentrations, it can damage biological permeability, ionic channels, receptors, and cell membrane enzymes.5 Cr(OH)₃⁡, Cr(OH)₄⁡, and Cr(OH)₃ chromyl ions prevail at pH levels below 3.6. When the pH is higher, Cr(III) precipitates as Cr(OH)₃·H₂O.⁶

The painting industry, including both surface plating and chromium electro-plating (decorative and hard plating), stainless steel handwork and other alloys, the concrete industry, etc., are the most important sources of Cr(VI) and Cr(III) compound waste.⁷

Currently, the methods for removing these ions are reduction and precipitation, adsorption and ion exchange, together with functional membranes.⁸⁹¹⁰

The most representative membrane technologies used for wasting solutions are reverse osmosis, ultrafiltration, nanofiltration, dialysis, diffusion dialysis, Donnan dialysis, membrane electrolysis, and electrodialysis (e.g., liquid, emulsified, and supported).⁹¹⁰

Donnan dialysis is an attractive membrane method that uses chemical potential differences between membrane sides to generate ionic transport and maintain the electro-neutrality of the two solutions.¹¹ Donnan dialysis can also be used to remove Cr(VI) ions with commercial anion exchange membranes such as SB-6470, AFN, ACM, and Raipore 1030.¹²

Areas such as chemical analysis for pre-concentration, extraction processes, hydrometallurgy, separating acids from their salts, radioactive flow deacidification, removal of copper and zinc using commercial cationic membranes, and removal of inorganic anions such as fluoride, nitrate, bromate, and borate from drinking water can all be achieved with Donnan dialysis.¹³⁻¹⁷

The development of new materials with definitive properties can include interpenetrating polymer networks (IPNs), which is an alternative method to modify microporous membranes. When two or more polymer networks are partially and non-covalently crosslinked on the molecular scale, it allows the formation of IPN architectures.¹⁸

IPN materials have many applications in biomedicine, water sorption, enzyme immobilization, ion exchange membranes, and fuel cells.¹⁹⁻²³

Chemically stable commercial porous materials are ideal for developing functional IPN membranes. Two examples of commercially available disposable membranes are micro-porous polypropylene (MPP) or polyethylene.²⁴ These polyolefin materials are attractive due to their thermal and mechanical stability and good chemical properties. It is also reported that poly[ar-vinylbenzyl] trimethylammonium chloride], P(ClVBTA), is effective for removing chromium ions.²⁵⁻²⁶ Poly[sodium (styrene sulphonate)], P(SSNa), is an efficient cation exchange polymer. P(SSNa) works to remove metal cations using a polymer-enhanced ultrafiltration technique.²⁷

The aim of this paper is to modify MPP support membranes by interpenetrating P(ClVBTA) and P(SSNa) networks and to study these membranes for the transport of Cr(VI) and Cr(III) ions, fitting this experimental data to a mathematical model that represents Donnan dialysis.

The development of a mathematical model that can predict target changes in solute concentration on both sides of a membrane is an attractive idea. The experimental data for Donnan dialysis were analyzed and adjusted to a theoretical mathematical model.

The mass transport process inside the modified membrane is controlled by Fick’s law (see Figure 1). Therefore, the first step is to determine the relationship between the extraction concentration and feed concentration of the target ion, following the linear relationship in equation 1.²⁸

\[ C_{ie} = c + b C_{if} \]  

where, the, Cᵢₑ is the target ion concentration in the extraction phase (mol L⁻¹); c, is the mathematical correction factor setting; Cᵢᵢ is the target ion concentration in the feed phase (mol L⁻¹); and b is the partition coefficient of the target ion in both aqueous phases.

Under no electrical current, the sum of the flux of feed ion (J) and driving ion (J) is zero, as in equation 2:

\[ z_i J_i + z_j J_j = 0 \]  

The Cr(VI) (see Figure 1 a), Cr(III) (see Figure 1 b), Na⁺, and Cl⁻ ions have different charge values (\( z_i \neq z_j \)). In this case, chromium driving ions diffuse through the membrane from the feed chamber to the extraction chamber. Under electron neutrality, the total concentration of all counterions in the membrane is equal to the fixed ions, which are denoted as the ion exchange capacity, as indicated in equation 3:

\[
  z_i C_i + z_j C_j = Q
\]

where the \( C_i \) and \( C_j \) are the anion and cation concentration inside the membrane (mol L\(^{-1}\)); \( Q \) is the ion exchange capacity (meq/g dry membrane\(^{-1}\)).

The membrane phase requires the following assumptions: a homogeneous material, charge density uniformly distributed throughout the structure, mass transfer process in a pseudo-steady state and in only one direction, control of separation that obeys Donnan equilibrium, a constant partition coefficient of counterions, and a very fast ion exchange reaction on the membrane surface.\(^{29}\)

The basic conditions of operation can help to identify the different control volumes that compose the Donnan dialysis system, for example, perfectly mixed aqueous solution phases (feed and extraction), constant phase density, environmental temperature, constant ion partition coefficient, constant volume (feed and extraction), and pseudo-steady-state operation.

If Donnan dialysis behavior is represented by the Nernst-Plank equation (eq. 4):

\[
  J_i = -D_i \frac{dC_i}{dx} + z_i C_i \frac{F \mu_i}{R T} \frac{dC}{dx} + q_i \nu
\]

where \( D_i \) is the ionic diffusion constant (m\(^2\) s\(^{-1}\)); \( \mu_i \) is the mass average velocity or convection velocity on the membrane (m s\(^{-1}\)); \( C_i \) is the concentration average of ions at the bulk solutions (mol L\(^{-1}\)); \( C \) is the concentration gradient respects to the thickness of the membrane (mol m\(^{-1}\) L\(^{-1}\)); \( L \) is the thickness of the membrane (m); and \( F, R \) and \( T \) are the Faraday constant (Coulombs mol\(^{-1}\)), gas constant (J K\(^{-1}\) mol\(^{-1}\)) and Temperature (Kelvin).

Equation 4 evaluates the solute fluxes just inside the membrane, and the convective contribution (\( \nu \)) is negligible. The analytical solution to the Nernst-Plank equation is in the extraction chamber (eq. 5):

\[
  C_{ig} = \frac{C_0}{z} \left( 1 - e^{-\frac{L}{\lambda}} \right)
\]

where \( C_{ig} \) is the target ion concentration in feed phase at time zero (mol L\(^{-1}\)); \( L \) is the the thickness of the membrane (m); \( \lambda \) is the time constant (minute).

Equation 5 substituted into equation 1 to obtain an equation for the feed concentration as a function of time in equation 6:

\[
  \frac{1}{b}[k (1 - e^{-\alpha t}) - c] = C_{if}
\]

where \( \alpha \) is the rate of response of the membrane by the diffusion (minute); \( k \) is the value of the equilibrium concentration by the target ion in the extraction phase (mol L\(^{-1}\)); \( V \) is the volume (m\(^3\)); \( S \) is the area of the membrane (m\(^2\)). Parameter (\( \lambda \)) was determined using a linearized equation 6 and then a least squares method. The solution was equation 10:

\[
  -\alpha = \frac{\text{cov}(\text{In}(C_{ig}+k),t)}{\text{var}(t)}
\]

The initial and boundary conditions for target ion \((C_{i}(x,t))\) are

\[
  C_{i}(x,0) = 0
\]

\[
  C_{i}(0,t) = K C_{if}(t)
\]

\[
  C_{i}(L,t) = K C_{ie}(t)
\]

\[
  C_{if}(0) = C_{0if}
\]

\[
  C_{ie}(0) = 0
\]

where \( C_{ie} \) is the chromium ion concentration (mol L\(^{-1}\)); \( x \) is the distance inside the membrane structure (m); \( L \) is the the thickness of the membrane (m); \( t \) is the time (s); and \( K \) is the partition coefficient of the membrane phase.

![Figure 1](figure1.png)

**Figure 1.** Mass balance scheme through modified membranes. a. Cr(VI) ion transport using P(CIVBTA) networks; b. Cr(III) ion transport using P(SSNa) networks.

**EXPERIMENTAL SECTION**

**Reagents and materials**

MPP membranes (0.6-μm pore size, AN06 Merck Millipore) were used. Sodium styrene sulphonate (SSNa, Aldrich), ammonium persulphate (APS, Merck), ar-[{vinylbenzyl]trimethylammonium chloride} (CIVBTA, Aldrich) and N,N-methylene bis acrylamide (MBA, Aldrich) were used for IPN synthesis. The other reagents used to modify the membrane surfaces were 15 kDa polyvinyl alcohol (PVA, Merck), 15 kDa poly(ethyleneimine) (PEI, Aldrich), glutaraldehyde (Ga) (Aldrich), divinylsulphone (Aldrich), 200 kDa poly(aryl-{[vinylbenzyl]trimethylammonium chloride}) (P(CIVBTA), Sigma-Aldrich), 200 kDa poly(sodium 4-styrenesulphonate) (P(SSNa), Aldrich), ethanol (Merck), and Type I deionized water from Thermo Fisher TKA Scientific. Potassium dichromate (Cr(VI), Merck) and chromium (III) nitrate nonahydrate (Cr(III), Merck) were the chromium sources. Hydrochloric acid (Merck), nitric acid (Merck), and sodium hydroxide (Merck) were used to adjust the pH. A UB-10 pH/mV meter from Denver Instruments was used to measure the pH. Sodium chloride (Merck) was used as the extraction agent.

A stirred-cell filtration unit (Millipore, model 8050) was used to inject the reactive solution into the MPP membrane pores. An aluminum flat reactor was used for radical polymerization.

A dielectric barrier discharge (DBD) plasma reactor was used to activate...
the membrane surfaces. The components and operating modes of the DBD were previously published. A Cary 100 scan UV-visible spectrophotometer from Varian was used to directly measure the Cr(VI) and Cr(III) ion concentrations. The Cr(VI) ion concentration was measured at 350 and 372 nm at pH 3.0 and 9.0, respectively. The Cr(III) ion concentration was measured at 407 and 573 nm for acidic pH. Origin® Pro 8 software was used to draw the profile graphics, and mathematical modeling was performed using R statistical software.

**Synthesis of P(CIVBTA) and P(SSNa) interpenetrating polymer networks**

An aqueous mixture of 50% w/w ethanol was used to wash the membranes and wet the pores. The functional monomer (CIVBTA or SSNa), crosslinking reagent (MBA), and initiator reagent (APS) in a 10-mL reaction solution were passed through the membrane using a stirred-cell filtration unit with nitrogen gas and a pressure of 1 bar. APS (1 mol %) was used as the radical initiator. The “in situ” free-radical polymerization was performed inside the membrane pores at 70°C for 24 h. The samples were dried in an oven at 50°C and stored in a silica dryer for 24 h. Table 1 shows the experimental design of IPN formation. For MC6 and MA7 membranes, both sides of the polypropylene membrane contacted the plasma argon for 1 min using plasma activation.

### Table 1. Experimental design of interpenetrating polymer network (IPN) synthesis inside pore polypropylene membranes.

<table>
<thead>
<tr>
<th>Sample code</th>
<th>Crosslinker / % MBA</th>
<th>Monomer / mol L⁻¹</th>
<th>Number of injections at 1 bar</th>
<th>Polymer</th>
</tr>
</thead>
<tbody>
<tr>
<td>MC1</td>
<td>2</td>
<td>4.0×10⁻¹</td>
<td>1</td>
<td>P(SSNa)</td>
</tr>
<tr>
<td>MC2</td>
<td>6</td>
<td>4.0×10⁻¹</td>
<td>1</td>
<td>---</td>
</tr>
<tr>
<td>MC3</td>
<td>6</td>
<td>4.0×10⁻¹</td>
<td>1</td>
<td>200 kDa</td>
</tr>
<tr>
<td>MC4</td>
<td>8</td>
<td>4.0×10⁻¹</td>
<td>1</td>
<td>200 kDa</td>
</tr>
<tr>
<td>MC5</td>
<td>4</td>
<td>4.0×10⁻¹</td>
<td>1</td>
<td>200 kDa</td>
</tr>
<tr>
<td>MC6</td>
<td>6</td>
<td>4.0×10⁻¹</td>
<td>---</td>
<td>---</td>
</tr>
</tbody>
</table>

**Characterization**

The characterization of the modified interpenetrating polymer networks membrane samples was developed through:

**Volumetric flux**

The time required for 50 mL of distilled deionized water to pass through a modified membrane was measured. A pressure of 1 bar was maintained for all tests. A stirred-cell filtration unit (Amicon) was used during this step using nitrogen gas as the pressure source.

**Modification degree**

The modification (% ΔGₚ) was measured gravimetrically. First, the unmodified membranes were weighed. These membrane samples (dried samples) were weighed after the modification. The % ΔGₚ was determined from equation 16:

\[
\% \Delta G_p = \frac{(w_f - w_d)}{w_o} \times 100 \quad (16)
\]

where \( w_f \) is the dry IPN membrane weight (g) and \( w_d \) is the unmodified membrane weight (g).

**Water uptake percentage**

The weight of the dry IPN modified membrane was measured before wetting with distilled deionized water for 24 h. During this period, the samples reached swelling equilibrium, and all tests occurred at room temperature. The excess water was removed from the modified wet membranes using absorbent paper in all tests. The weight of the modified membranes was measured three times. The water uptake percent (% ΔWₚ) was calculated from equation 17:

\[
\% \Delta W_p = \frac{(w_w - w_d)}{w_d} \times 100 \quad (17)
\]

where \( w_w \) is the wet IPN membrane weight (g) and \( w_d \) is the dry IPN membrane weight (g).

**Scanning Electron Microscopy (SEM)**

This technique was used to analyze the morphological changes in the modified and unmodified membranes. A 20000 kV JOEL microscope (JSH6380LV model) was used.

**Charge density properties**

Brookhaven Zeta Plus equipment was used. The samples were cut into thin pieces and submerged in 0.05 M KCl at pH 3.0, 5.0, 7.0, and 9.0. The pH was controlled using HCl and NaOH. The electrokinetic potential (ζ) was determined from the ionic mobility (\( \mu_e \)) using the Smoluchowski Equation (eq. 18):

\[
\mu_e = \frac{\varepsilon \sigma}{\eta} \quad (18)
\]

where \( \varepsilon \) is the permittivity [J V⁻¹ m⁻¹], \( \sigma \) is the electrical conductivity [S m⁻¹], \( \eta \) is the liquid viscosity, \( \mu_e \) is the ionic electrophoretic mobility [m² V⁻¹ s⁻¹], \( C \) is the KCl concentration, and \( \sigma^* \) is the charge density.

Table 1 shows the experimental design of IPN formation. For MC6 and MA7 membranes, both sides of the polypropylene membrane contacted the plasma argon for 1 min using plasma activation.
**Experimental design**

Modified membranes with P(CIVBTA) networks were used for Cr(VI) ion transport, and modified membranes with P(SSNa) networks were used to study Cr(III) ion transport. For Cr(III) ions, the feed chamber was filled with the Cr(III) acid solution, and the extraction chamber was filled with HNO$_3$ solution. In other experiments, the extraction chamber was filled with a mixture of 1 M NaCl and 0.01 M HNO$_3$. Samples were removed from the extraction chamber to measure the Cr(III) ion concentration. 3 mL sample was taken every 60 min for 4 and 6 h. Direct UV-visible spectrophotometry was used to measure the Cr(III) ion concentration. For Cr(VI) ion, the feed chamber was filled with the Cr(VI) solution, and the extraction chamber was filled with a 1 M NaCl solution. Every 60 min for 18 to 24 h, 3 mL was extracted from the extraction chamber. Direct UV-visible spectrophotometry was used to measure the Cr(VI) ion concentration. The samples were returned to the extraction chamber after measuring the Cr(VI) ion concentration. Table 2 shows the experimental conditions for the transport study.

Table 2. Experimental conditions to evaluate Cr(VI) and Cr(III) ion transport.

<table>
<thead>
<tr>
<th>Experiment</th>
<th>[Cr(III)] /mol L$^{-1}$</th>
<th>pH$_{\text{feed phase}}$</th>
<th>pH$_{\text{extraction phase}}$</th>
<th>Extraction agent / mol L$^{-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>/P(SSNa)</td>
<td></td>
<td></td>
<td></td>
<td>[HNO$_3$] [NaCl]</td>
</tr>
<tr>
<td>1</td>
<td>4×10$^{-2}$</td>
<td>2.0</td>
<td>1.0</td>
<td>1×10$^{-1}$ --</td>
</tr>
<tr>
<td>2</td>
<td>4×10$^{-2}$</td>
<td>2.0</td>
<td>2.0</td>
<td>1×10$^{-2}$ 1</td>
</tr>
<tr>
<td>P(CIVBTA)</td>
<td></td>
<td></td>
<td></td>
<td>[NaCl]</td>
</tr>
<tr>
<td>3</td>
<td>5×10$^{-4}$</td>
<td>3.0</td>
<td>3.0</td>
<td>1</td>
</tr>
<tr>
<td>4</td>
<td>5×10$^{-4}$</td>
<td>9.0</td>
<td>9.0</td>
<td>1</td>
</tr>
</tbody>
</table>

**RESULTS AND DISCUSSION**

**Characterization**

The volumetric flux of water by the modified membranes was low relative to the MPP sample for both anionic and cationic membranes. Figure 2a shows the tendency of volumetric water flux through membranes modified with P(SSNa). In zone I, the volumetric flux of MPP is indicated as a reference, while in zone II, the passage of water is influenced by the number of injections and the MBA concentration of the MC1 and MC2 membranes. The resistance to water flux was higher for MC2 because the mass of P(SSNa) increased more inside the structure compared to MC1. Zone III (MC3, MC4, and MC5 membranes with P(SSNa) 200 kDa, linear) shows resistance to volumetric flux, which increases independent of MBA quantity. It is possible that the internal morphological structure of MPP leads to this irregularity. The result for MC6 (zone IV) is very similar to that of zone III. The lowest volumetric flux for membranes modified with P(SSNa) is in MC2. In general, this can be attributed to the P(SSNa) IPN morphology in the layer shape. These results will be shown in the SEM analysis.

Figure 2b shows five representative zones that depend on the method, synthesis conditions and internal morphological structure of MPP. Zone I is the reference parameter of the MPP. Zone II (MA1, MA2 and MA3) shows modified membranes with changes in the injection number and CIVBTA concentration. The decrease in volumetric flux in this zone depends mainly on the monomer CIVBTA concentration. The minimum volumetric flux values are obtained in zones III and V. This was achieved for MA4 and MA7, which are modified membranes with 6 mol % of MBA crosslinking agent but different methods of preparation. The internal structure and initial pore distribution of MPP may control the growth of P(CIVBTA) polymer networks.

In zone IV (MA5 and MA6, membranes with 200-kDa P(CIVBTA)), it is possible to observe a reversal in the volumetric flux trend that increased when the MBA crosslinking agent was used. This may be due to the formation of domains that separate the phases due to hydrophobic repulsion between the polypropylene and hydrophilic networks.

The change in volumetric water flux decreased for these modified membranes because P(SSNa) and P(CIVBTA) IPN grew inside the pores and produced resistance to water. This is the first evidence of the modification process. The P(SSNa) IPNs were deeper for the PP membrane than the P(CIVBTA) IPNs. This is why it is easier to access quaternary ammonium groups. These results are supported by SEM analysis.
The evaluation of the modified MPP membranes must consider the change in the modification percent degree and the water uptake percentage. These tests confirm the complete modification. Figure 3a shows the tendency of the modification percent degree, and in zones I, II, and III, these values increased as a function of MBA concentration. The highest percent modifications for all of the synthesized P(SSNa) IPN membranes were achieved for MC6 (3.53%), MC5 (3.52%), and MC1 (3.36%). However, the water uptake percentages were not homogeneous and do not follow the tendency of the modification percent degree. The modifications (%) of the MC1 and MA2 (see Figure 3b) membranes were similar, while their percent water uptake and volumetric fluxes were smaller for higher injection quantities.

Zone I in Figure 3b shows that the modification percent degree increases with the ClVBTA monomer concentration in contrast to the water uptake percentage. If the concentrations of P(ClVBTA) networks increase and the internal space of the MPP decreases, the functional networks cannot swell freely. The MA1 and MA2 membranes had increasing percent modifications because they are a function of injection number and monomer concentration, but if the monomer concentration is $6.0 \times 10^{-1} \text{ mol/L}$ (MA3), only one injection is necessary. Zone III and zone I have the same tendencies.

The highest percent modification for IPN membranes with the change in monomer concentration and injection number was achieved by MA3 (5.27%), while the highest percent modification for the semi-IPN membranes was achieved by MA5 (4.38%), and the highest change in MBA percent for IPN was achieved by MA4 (3.5%) and MA7 (4.1%). Similar results are obtained in zones II and IV.

The membranes synthesized via a superficial activation plasma technique (MC6 and MA7) exhibited percent modifications, percent water uptake, and water volumetric flux changes that are similar to those of the semi-IPN membranes (MC5 and MA6).

**Figure 3.** Optimum values of modified degree, $\% \Delta G_m$, and water uptake percentage, $\% \Delta W_w$.

**Figure 4.** SEM images. MPP (a. superficial face to 50 µm, and $\times 300$. b. Cross-sectional area to 50 µm, and $\times 300$. c. Cross-sectional area close to the superficial face to 5 µm, and $\times 3000$). MA4, modified membrane with P(ClVBTA) (d. superficial face to 50 µm, and $\times 300$. e. Cross-sectional area to 50 µm, and $\times 300$. f. Cross-sectional area close to the superficial face to 5 µm, and $\times 3000$). MC2, Modified membrane with P(SSNa) (g. superficial face to 50 µm, and $\times 300$. h. Cross-sectional area to 50 µm, and $\times 300$. i. Cross-sectional area close to the superficial face to 5 µm, and $\times 3000$).
The membrane morphologies of the P(CIVBTA) and P(SSNa) network membranes were compared to the unmodified MPP membrane. Figure 4a shows the morphology of unmodified MPP in which the membrane face had an intertwined fiber structure, low porosity, and a smooth superficial aspect. In contrast, the cross-sectional area shows high density, based on the thick and compacted PP fibers (see Figure 4b). These results represent an anisotropic membrane (see Figure 4c).33

The highest P(CIVBTA) network concentration was found on the superficial face relative to the observed membrane cross-section. Figures 4d, e, and f show the results of the representative MA4. For example, in Figure 4d, two different phases were observed: the first was the PP fibers, and the second was the P(CIVBTA) networks. Figure 4e shows the PP fibers that provide support and mechanical resistance to amorphous IPN materials, while the IPN materials produced the ion exchange. Additionally, these results indicate a change in micro-structural homogeneity (see Figure 4f) compared to the unmodified MPP membrane (see Figure 4c).

The morphology achieved in this investigation (P(CIVBTA) networks) was very similar to the results of the grafted and copolymerized 4-vinylpiridinium monomer within MPP membranes because they are pore-narrowing and pore-blocking; the smoother surface is covered by a thin polymer layer, and the surface membranes are evenly modified.34 This makes it possible to observe some places with the amorphous materials of the functional polymer.

The P(SSNa) network particles were smaller and less agglomerated than in the P(CIVBTA) network. This result is presented in Figures 4g, h, and i. The MC2 representative membrane exhibited two phases relative to the unmodified MPP membrane (see Figure 4g). The P(SSNa) was enclosed in the MPP structure and covered the entire MPP fiber surface like paint (see Figure 4h and i). In the cross-section region, this membrane maintains the same morphology as the MPP sample (see Figures 4b and g). The P(SSNa) networks were generally more homogeneous and covered more PP fibers than the P(CIVBTA) networks (see Figure 4i). In general, the membranes exhibited low IPN concentrations in their cross-sections due to the hydrophobic nature of the isotactic MPP and low pore uniformity due to their highly asymmetric character.33,34

SEM analysis of the polyethylene and polypropylene membranes modified by grafting P(SSNa) was superficially similar to the present results. The analysis found a structural surface change in which small particles with small pores appeared, indicating that the membrane surface was unevenly modified.37

**Charge density properties**

![Figure 5](image.png)

**Figure 5.** Charge density profile derivation of the electrokinetic potential of modified membranes: a. P(SSNa)-modified membranes; and b. P(CIVBTA)-modified membranes.

The MPP membrane is hydrophobic without any modification and has no ionic functional groups, which makes the membrane inert to electric fields. The superficial charge density distributions produced by the ionic functional groups were analyzed using the electrokinetic properties. Electrokinetic potential can be used to evaluate membrane stability, polyvalent ion absorption capacity, and pore size.35 The electrokinetic potential is the fixed charge potential difference (quaternary ammonium and sulfonate groups) between the mobile ionic charges in the absorption layer. The change in pH caused the networks to extend or compact their segments. The charge density values depend on previously described behavior.35

Figure 5a shows a tendency to decrease charge density in membranes modified with P(SSNa) networks when the pH increases. At pH 7.0 to 9.0, the excess OH\(^-\) ions repelled the sulphonate groups fixed in the network and favored the movement of the Na\(^+\) counterion in the diffusion layer. In this range, Donnan exclusion is favorable. At pH 3.0, the charge density properties become less negative because H\(^+\) ions compete with Na\(^+\) ions in the diffusion layer. The response signal of the membranes modified by an electric field depends on the modification percentage degree of the P(SSNa) IPN concentrations and the internal distribution. A more intense signal was achieved for MC5 and MC6 compared to the other test samples.

Figure 5b shows the profile of the charge density for membranes modified with P(CIVBTA) networks. These membranes exhibited high charge density when the pH was 3.0 and depend on the excess H\(^+\) repelling the quaternary ammonium groups. Between pH 5.0 and 9.0, the charge density decreases due to OH\(^-\) ions, which compete with Cl\(^-\) ions in the diffusion layer. The presence and movement of the Cl\(^-\) counterion in the diffusion layer is favored when the pH is 3.0.36 MA3 and MA5 membranes achieved high charge density.

The functional groups in P(CIVBTA) and P(SSNa) were electrically charged across the entire pH range.41 In general, if the functional IPN concentration is high, the water uptake percent is low because the hydrophobic character increases, and the superficial charges inside the membrane cannot be reached by the ionic solution.

**Ion transport evaluation using Donnan dialysis**

The mathematical model for the behavior of Cr(III) was evaluated using the correlation coefficient (R\(^2\)), which was close to 1 in all tests. R\(^2\) was low for MPP only when using NaCl for extraction (see Table 3). The concentration polarization effect was neglected due to the sufficiently high stirring speed in each cell chamber. Similar results were obtained when the experimental data of the Cr(III) ions were fitted to a non-linear curve as the exponential mathematical model using the Leveberg-Marquardt algorithm.42

Figure 6 shows the mathematical model fit by the Cr(III) ions at pH 2.0 in the feed phase, and the extraction phase at pH 1.0. Cr(III) can exist as CrOH\(^+\) and Cr(OH)\(_2\)\(^+\) at 0.04 mol/L.43,44 The acidity guarantees total dissolution and Cr(III) ionization, which prevents the formation of solid precipitate.45 The Donnan equilibrium for MC1 (see Figure 6a), MC2 (see Figure 6b), MC5 (see Figure 6c), and MC6 (see Figure 6d) membranes was achieved between 250 and 500 minutes, and in the extraction profile curve, the Cr(III) concentration at equilibrium did not overcome the Cr(III) concentration at the equilibrium of the feed phase (see Figures 6 a, c, and d).
The (a) parameter obtained in the mathematical fitting can report the rate of response of the external Cr(III) ion concentration in both phases (feed and receiving).

To extract the Cr(III) ion in acid media under the first experimental condition, if the (k) parameter value is low, the (a) parameter value is high. The MC1 membrane follows this relationship. An inverse relation was obtained for the MC4 membrane. The results for the parameters (a, b, c, and k) from the mathematical model fit are shown in Table 3. Moreover, when the extraction contained chloride (experimental condition 2 for Cr(III)), the (k) and (a) parameters were higher than when extracting with nitric acid. When chloride was used as the extracting ion, the MC1 and MC4 membranes showed the same behavior as nitric acid alone.

The (b) parameter, which indicates the partition of the Cr(III) ion in both phases (feed and receiving), was very similar for both experimental conditions. In both cases, MC2 had the lowest value, and MC3 and MC6 gave high values.

Table 3. Constant values for the mathematical model fit using experimental data for Cr(III) extraction.

<table>
<thead>
<tr>
<th>Experimental condition</th>
<th>Sample</th>
<th>Estimated parameter</th>
<th>Adjustment</th>
</tr>
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<tbody>
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<td></td>
<td></td>
<td>k×10⁴</td>
<td>a×10⁻³</td>
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<tr>
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<td>197.4</td>
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Figure 7 shows the profile in both phases (feed and receiving) for Cr(III) when Na⁺ was used as the driving ion force that helped the H⁺ extracting ion. The Donnan equilibrium for MC1 (see Figure 7 a), MC2 (see Figure 7 b), MC5 (see Figure 7 c), and MC6 (see Figure 7 d) membranes was achieved between 300 and 450 min, and in the extraction profile curve, the Cr(III) concentration at equilibrium overcame the Cr(III) concentration at equilibrium in the feed phase. However, the modified membrane has a low effect on retaining the Cr(III) ions inside its structure.

The Na⁺ ion improved the extraction of the Cr(III) ions by 10% compared to H⁺ ion. The Na⁺ ion replaces or displaces the active sites of the Cr(III) ions inside the membrane. This effect was higher when the extraction used sodium ion rather than H⁺.

For pH 9.0 in both phases, the parameters from the fitting of the mathematical model are reported in Table 4. Figure 9 shows the mathematical model fitting. The model was evaluated using the R² value of both conditions and phases. Figure 9 shows the time to Donnan equilibrium. The dotted line indicates the mathematical curve fit for both phases, and the continuous line with points is the experimental data. At pH 9.0, Cr(VI) ion transport under such conditions depends on the pH(CIVBA) network concentration inside the pores; in acidic pH, the influence of percent modification is mainly due to the variation in porosity.

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Figure 6. Experimental data for the Cr(III) ion concentration in both phases (feed and receiving) fitted to the mathematical model using modified membranes with P(SSNa): a. MC1; b. MC2; c. MC5; d. MC6; and e. MPP at pH 2.0 in the feed phase and extraction phase at pH 1.0. H+ is the extracting ion.
Moreover, the (a) parameter for the transport of Cr(VI) ions shows higher values for the rate of response at pH 9.0 than at pH 3.0. The values of the (a) parameter depend on the internal morphology and modification percentage degree of the membranes because the internal structure can help the diffusion of Cr(VI). MA3 achieves the highest rate of response and MA7 the lowest. If the (a) parameter value is high, then the transport test is faster to achieve convergence of the (k) parameter, in both experimental conditions (pH 3.0 and pH 9.0).

The (b) parameter for the extraction at pH 9.0 indicates the partitioning of the Cr(VI) ions in the feed and extraction phases. The MA3 achieves low values for the (k) and (b) parameters, but a high value for the (a) parameter. It is possible that MA3 has retention behaviour in the internal structure. MA7 achieves high values for the (b) and (k) parameters, but a low value for the (a) parameter. The morphology of the functional network change depends on the pH of the solution. Moreover, MA4 and MA6 achieve very similar values of (b). The Stokes radius of hydration of Cr(VI) at pH 3.0 (HCrO$_4^-$, 0.375 nm) and pH 9.0 (CrO$_4^{2-}$, 0.240 nm) produce one effect in the transport through the membranes because the size difference causes friction during the movement and a strong electrostatic force during the ion exchange. All of these features produce a retention effect.

The (c) parameter in the mathematical model fitting has the function of the correction of the fitting. This parameter can be understood as an approximation of the extraction target ion concentration when the feed phase does not have the target ion concentration. The main function of (c) is to reduce the slant and the error of the fitting to zero. If the (c) parameter is not considered, the error value will be the (c) constant. These results are shown in Table 3 and Table 4.

Figure 7. Experimental data for the Cr(III) ion concentration in both phases (feed and extraction) fitted to the mathematical model using modified membranes with P(SSNa): a. MC1; b. MC2; c. MC5; and d. MC6 at pH 2.0. Na$^+$ is the driving ion force that assists the H$^+$ extracting ion.
CONCLUSIONS

Modified MPP membranes with P(CIVBTA) and P(SSNa) have ion exchange capacities and can be obtained using radical polymerization. The crosslinker reagent concentrations can control the functional network density, as demonstrated using SEM, volumetric flux, and water uptake percentage.

When Cr(III) transport was analyzed and 0.1 mol/L HNO₃ was used as the extraction agent, MC4 achieved the highest extraction because the value of k (138.6×10⁻⁴) is highest in comparison with the other functional P(SSNa) membranes tested. However, when Cr(III) transport was analysed and a 0.01 mol/L HNO₃ and 1 mol/L NaCl mixture was used as the extraction agent, MC4 achieved the highest extraction because the k value (198×10⁻⁴) is highest in comparison with the other functional P(SSNa) membranes tested. However, MC4 achieved an (a) value of -9.69×10⁻³, which is not the lowest.

For Cr(VI) transport at pH 3.0, MA6 achieved the highest extraction because the value of k (1.79×10⁻⁴) is highest in comparison with the other functional P(CIVBTA) membranes tested. However, when Cr(VI) transport was analysed pH 9.0, MA7 achieved the highest extraction because the k value (3.55×10⁻⁴) is highest in comparison with the other functional P(CIVBTA) membranes tested.

ACKNOWLEDGEMENTS

The authors thank FONDECYT (Grant No 1150510). Julio Sánchez thanks FONDECYT (Grant No 11140324) and DICYT (Grant No 021741SP), VRIDEI, Universidad de Santiago de Chile.
### Table 4. Constant values of the mathematical model fit using the experimental data for Cr(VI) extraction.

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**Figure 9.** Experimental data’s of the Cr(VI) ions concentration in both phases (feed and extraction) fitted to the mathematical model at pH 9.0, using the modified membranes with Pr(CIVBTA). a. MA3. b. MA5. c. MA7. d. MPP.